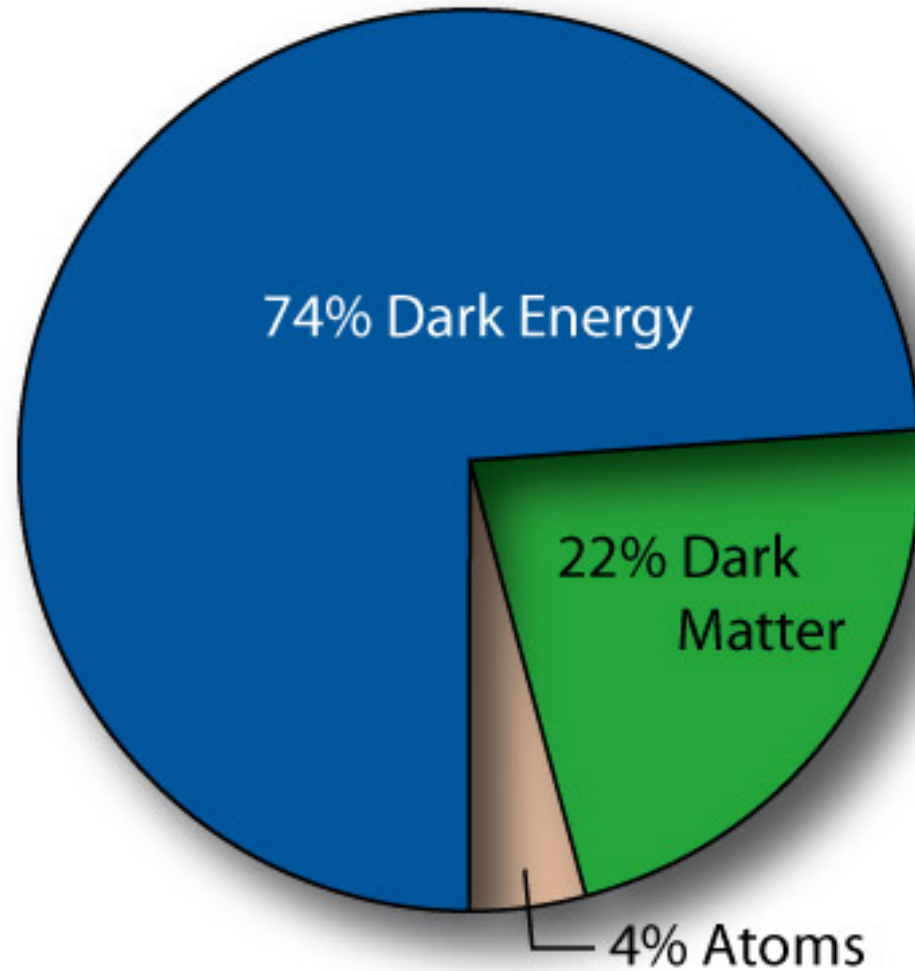


ダークマターとCTA

Kazunori Kohri (郡 和範)

Physics Department, Tohoku University

Dark Matter?



$$\Omega_i \equiv \frac{\rho_i}{\rho_c} \Big|_0$$
$$\Omega_{\text{CDM}} h^2 \sim 0.1$$

What is Dark Matter?

- It is massive ($\rho \propto a^{-3}$)
- It is stable ($\tau \gg 10^{18}$ sec)
- It does not scatter off photons so much
(Is it a bound-state?)
- It is neutral
(from experiments of sea water $m < 10^6$ GeV)
- The velocity dispersion is small [cold dark matter (CDM)]

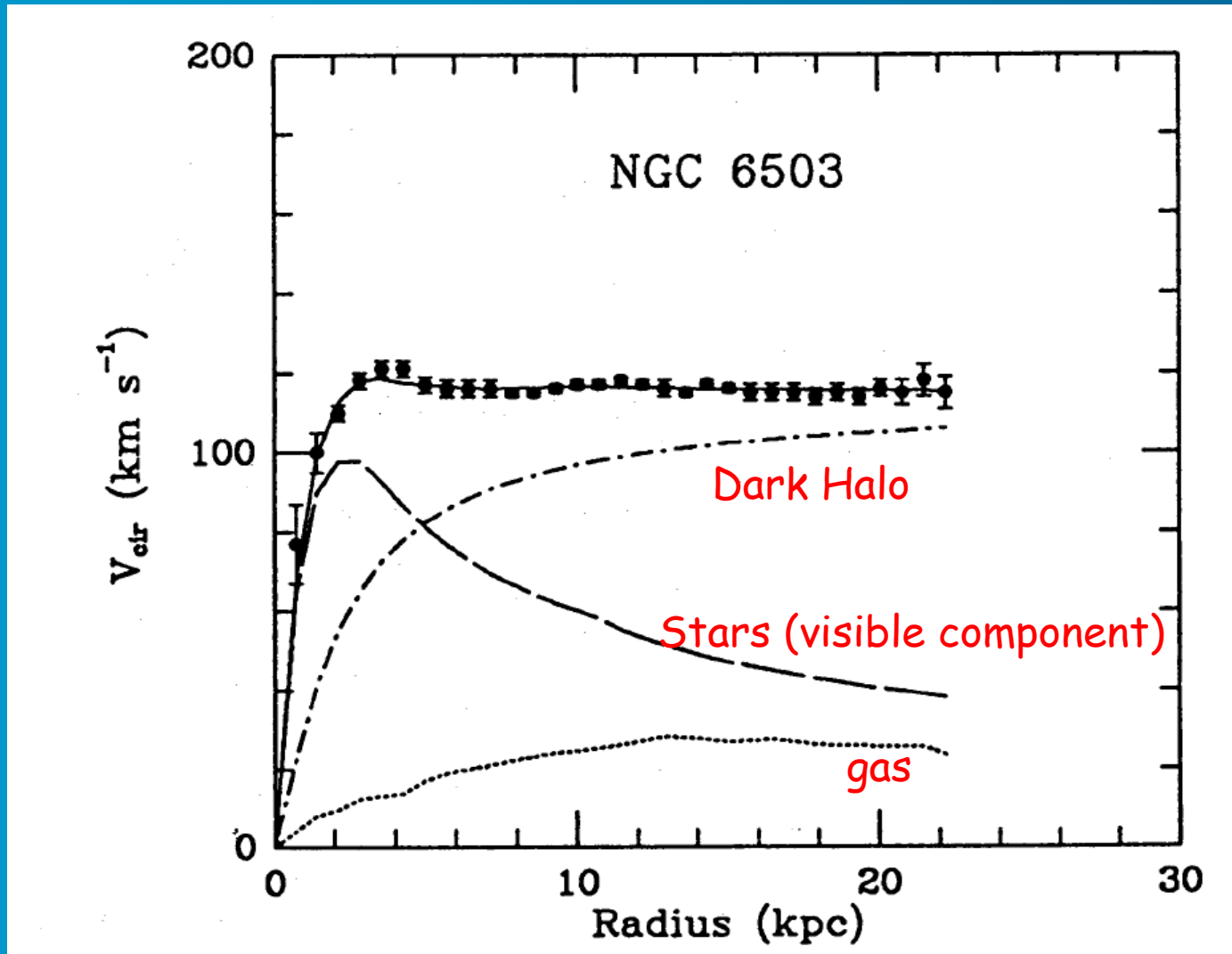
Candidate of particle (cold) dark matter

- Stable or long-lived new particle
 - Neutralino
 - Gravitino
 - Right-handed sneutrino
 - Axino
 - ...
- Oscillating scalar field
 - Axion
 - Moduli
 - ...

Another candidates

- Primordial black hole
- Brown dwarf
- WIMPZILLA
- Integral constant in Horava-Lifshitz gravity
- Quark nugget (strange-quark matter)
- Solutions in (relativistic-) Modified Newtonian Dynamics (MOND)
- ...

Rotation curve

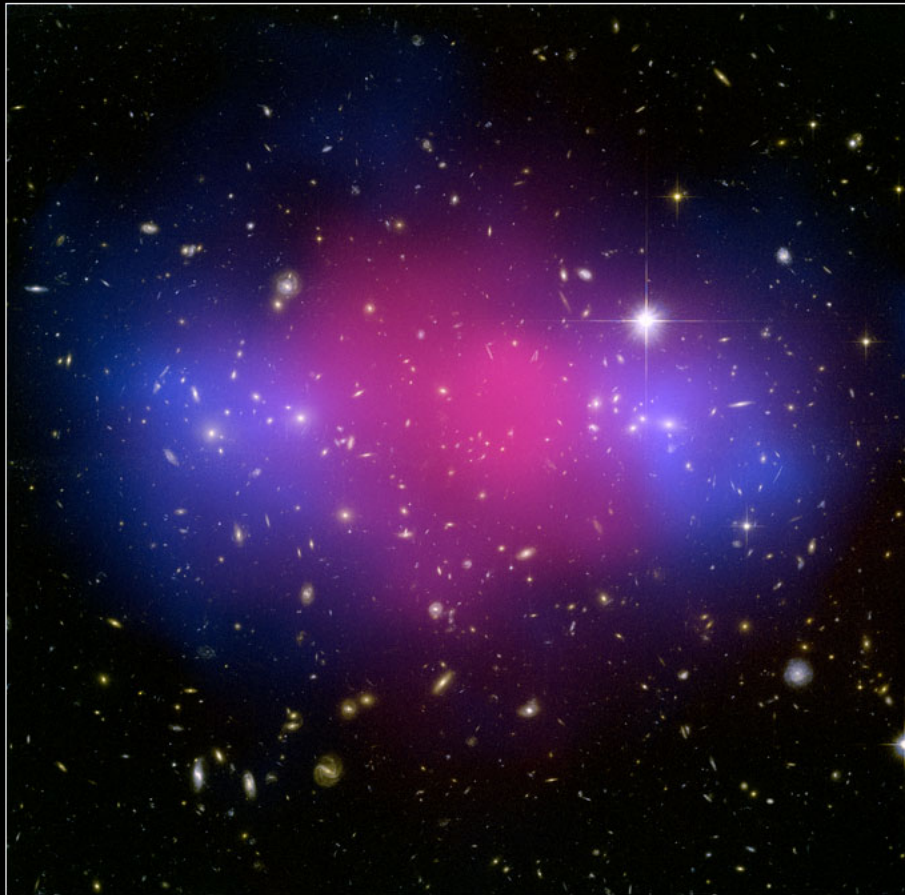


$$M(r) \propto r$$

Begeman, Broils, Sandars et al (91)

Gravitational lens in colliding cluster of galaxies

Dark Matter in Galaxy Cluster MACS J00254.4-1222 HST ACS/WFC • CXO



NASA, ESA, CXO, M. Bradač (University of California, Santa Barbara), and S. Allen (Stanford University)

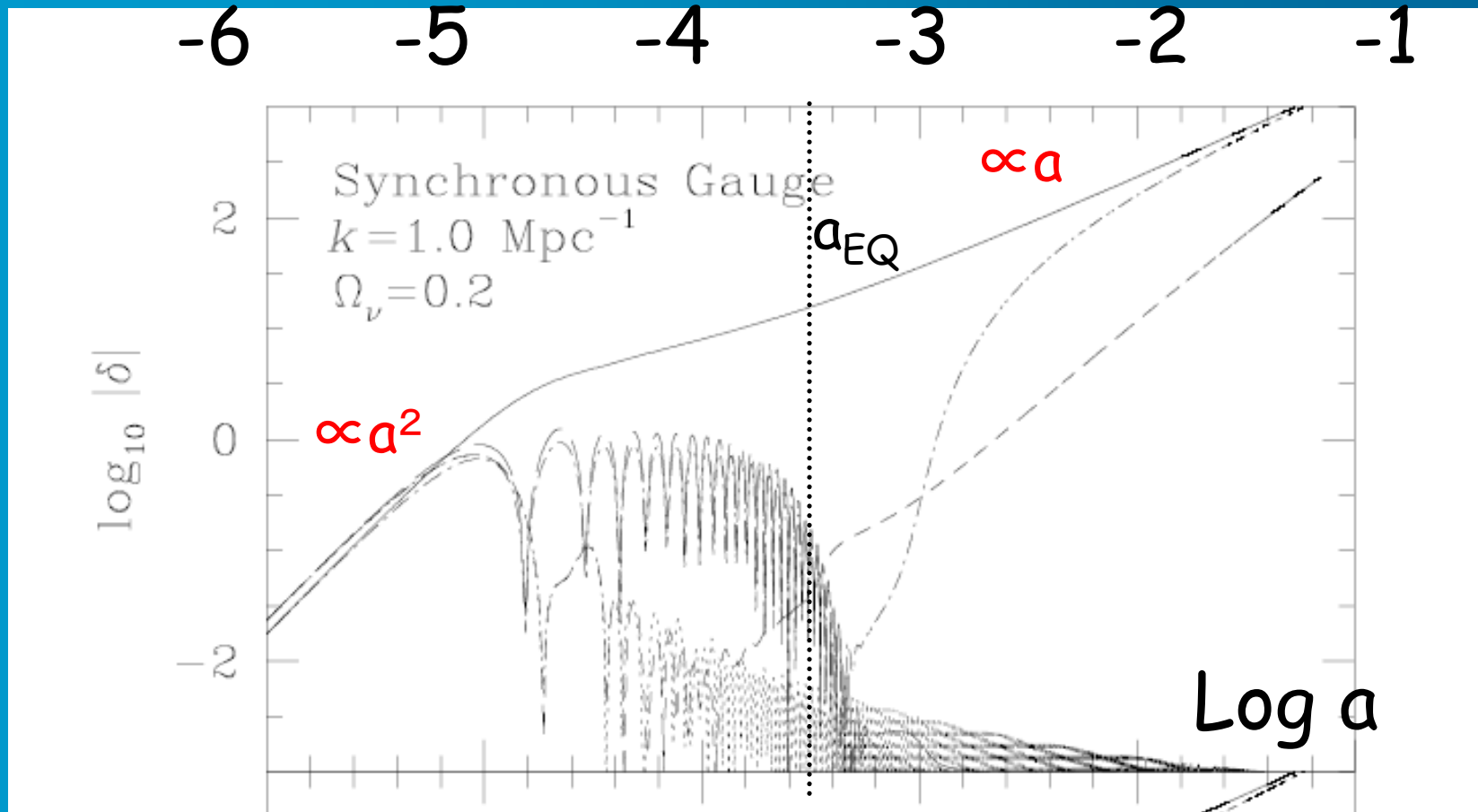
STScI-PRC08-32

- Red: Baryon observed by X-ray produced by brems of thermal electron
- Blue: DM observed by gravitational lens

(2007)

Time-evolution of fluctuation III

(II) Horizon reentry before matter-radiation equality epoch



Ma and Bertschinger (95)

See also 松原隆彦「シリーズ 現代の天文学3 宇宙論 II 宇宙の進化」

Cluster baryon fraction

- Cluster can have a representative distribution in the Universe of both baryon and DM

$$f_b = \frac{\Omega_b}{\Omega_m} \simeq f_{\text{gas}} + f_{\text{gal}}$$

- $\Omega_b h^2$ is independently known, f_{gas} was observed by X-ray from Oxygen

$$\Omega_m = \frac{\Omega_b}{f_{\text{gas}} + f_{\text{gal}}} \simeq \frac{\Omega_b}{0.08h^{-1.5} + 0.01h^{-1}}$$

$$\Omega_m \sim 0.2$$

Combined Figure

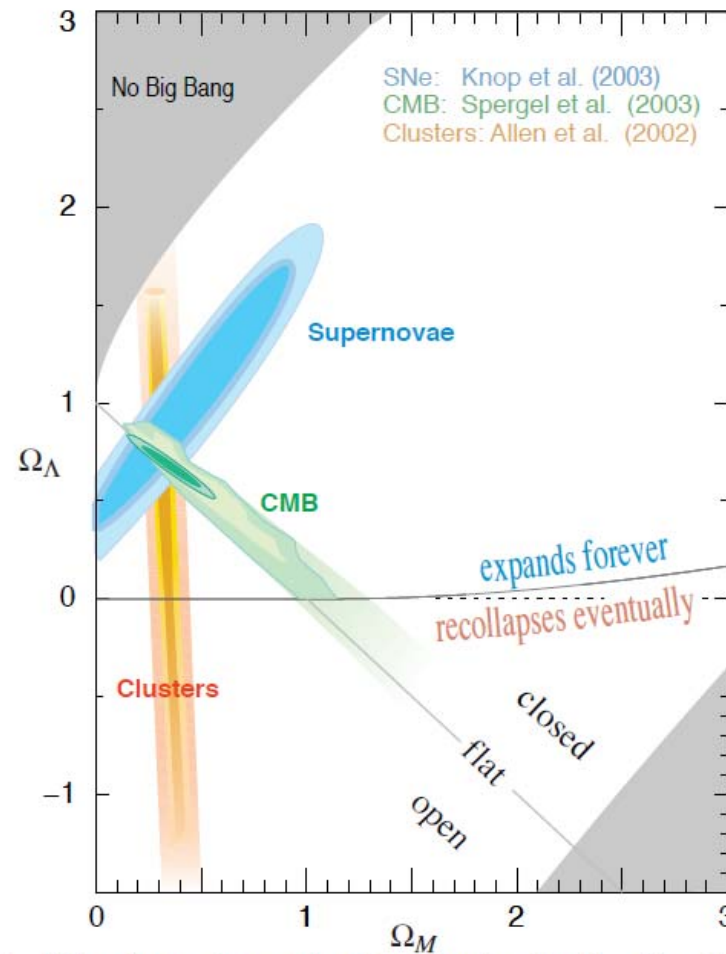
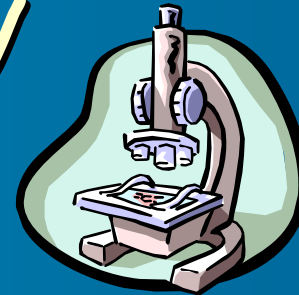


Figure 21.1: This shows the preferred region in the Ω_m - Ω_Λ plane from the compilation of supernovae data in Ref. 18, and also the complementary results coming from some other observations. [Courtesy of the Supernova Cosmology Project.]

Riess et al (98), Lahav-Liddle PDG (09)

Introduction to SUSY



✚ Supersymmetry (SUSY)

- Solving "Hierarchy Problem"
- Realizing "Coupling constant unification in GUT"

Fermion ↔ Boson

quark ↔ squark

lepton ↔ slepton

photino ↔ photon

neutralino

gravitino ↔ graviton

Depending on SUGRA models

Hierarchy Problems

- GUT-scale

$$M_X \approx 10^{14} - 10^{15} \text{ GeV}$$

- Weak-scale

$$M_W \approx 10^2 - 10^3 \text{ GeV}$$

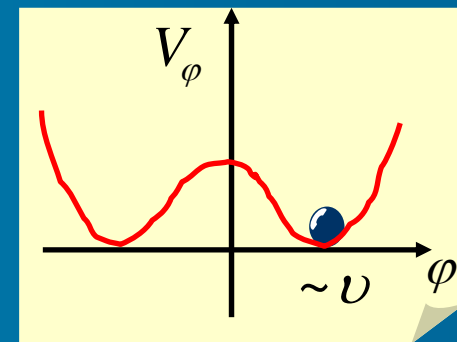
12-13 orders of magnitude !!!

Higgs mass

$$m_{\phi^0}^2 = \frac{d^2 V_\phi}{d\phi^2} \approx \lambda v^2 \approx O(M_W^2)$$

where Higgs's potential

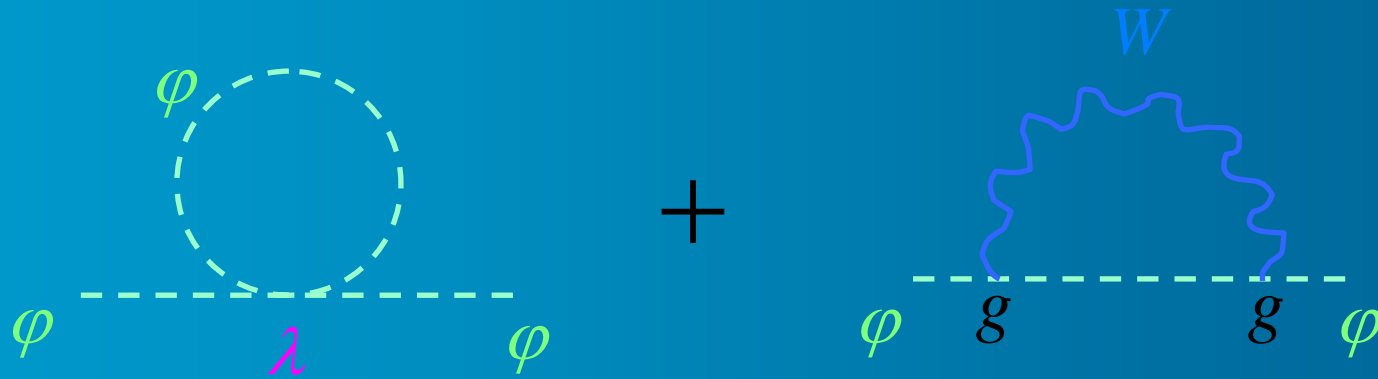
$$V_\phi = \lambda \left(\phi^\dagger \phi - v^2 / 2 \right)^2$$



c.f) Masses of fermions and vector bosons

$$m_\psi \sim h_\psi \langle \phi \rangle, \quad m_Z \sim g \langle \phi \rangle$$

Radiative correction to Higgs mass in Quantum Field Theory



$$\delta m_{\varphi}^2 \sim \lambda \Lambda^2 + g^2 \Lambda^2 \quad \leftarrow \quad \boxed{\text{Quadratic divergence}}$$

Cut off scale $\Lambda \sim M_X \sim 10^{15} \text{ GeV}$

$$\boxed{\delta m_{\varphi}^2 \sim (10^{15} \text{ GeV})^2 ?}$$

How can we resolve the problem?

Weak scale in the tree level, $m_{\varphi 0}^2 \sim (10^2 \text{ GeV})^2$


In total, $\delta m_{\varphi}^2 \sim (10^{15} \text{ GeV})^2$

$$m_{\varphi}^2 \sim m_{\varphi 0}^2 + \delta m_{\varphi}^2 \sim (10^{15} \text{ GeV})^2 ?$$

To retain the hierarchy, we require an accidental cancellation,

$$m_{\varphi 0}^2 + \delta m_{\varphi 1}^2 + \delta m_{\varphi 2}^2 + \delta m_{\varphi 3}^2 + \dots \sim (10^2 \text{ GeV})^2 ?$$

$[O(10^{15} \text{ GeV})]^2$



GDP in USA (2002)?

\$ 10,110,087,734,958.95

-) \$ 10,110,087,734,957.70

\$ 1.25

Fine tuning!

Solution in SUSY

In exact SUSY, the quadratic divergence is canceled by both boson and fermion loops.

$$\begin{aligned}
 & \varphi \text{ --- } \left[\text{Feynman diagram: fermion loop } t \text{ with vertices } h_t \right] \text{ --- } \varphi & + & \quad \varphi \text{ --- } \left[\text{Feynman diagram: boson loop } \tilde{t} \text{ with vertex } h_t^2 \right] \text{ --- } \varphi & = & \quad 0 \\
 & - \frac{1}{(4\pi)^2} h_t^2 \Lambda^2 & & & \frac{1}{(4\pi)^2} h_t^2 \Lambda^2 & & \text{Exact SUSY}
 \end{aligned}$$

Even if ~~SUSY~~,

$$\delta m_\varphi^2 \sim \frac{1}{(4\pi)^2} h_t^2 m_{\tilde{t}}^2 \ln \left(\frac{\Lambda^2}{m_{\tilde{t}}^2} \right)$$

We don't need a fine tuning when

$$m_{\tilde{t}}^2 \sim m_{\tilde{b}}^2 \sim \dots \sim O(M_W^2)$$

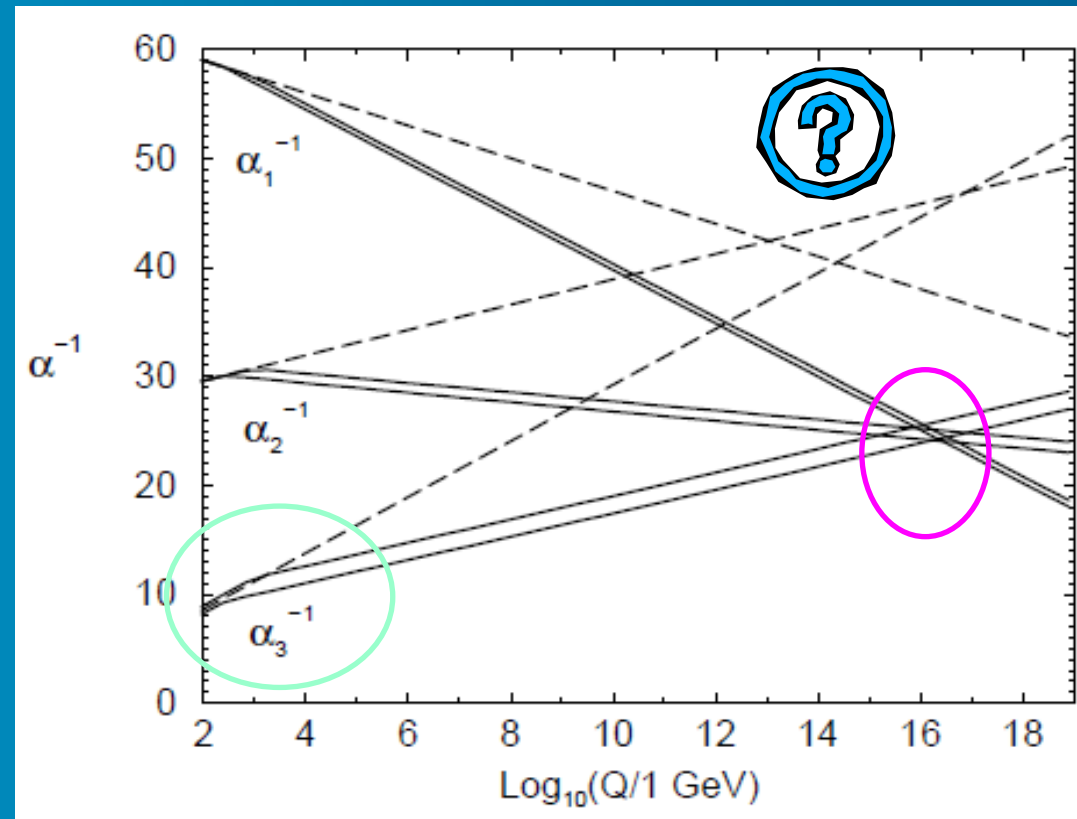
SUSY GUT

The coupling constants
are unified at

$$M_x \approx 10^{16} \text{ GeV}$$

A lot of new
particles, which do not obey
the asymptotic free, appear
at

$$\mu \geq 10^2 \text{ GeV}$$



Martin, "A Supersymmetry Primer"

Lightest SUSY particle (LSP)

- R-parity conservation

i) Decay

$$\tilde{\tau} \rightarrow \chi + \tau$$

$$(-1) \quad (-1) \quad (+1)$$

ii) Pair annihilation/production

$$f + \bar{f} \leftrightarrow \chi + \chi$$

$$(+1) \quad (+1) \quad (-1) \quad (-1)$$

Thermal freezeout

Boltzmann equation

$$\frac{dn_\chi}{dt} + 3Hn_\chi = -\langle\sigma_{AV}\rangle [(n_\chi)^2 - (n_\chi^{\text{eq}})^2]$$

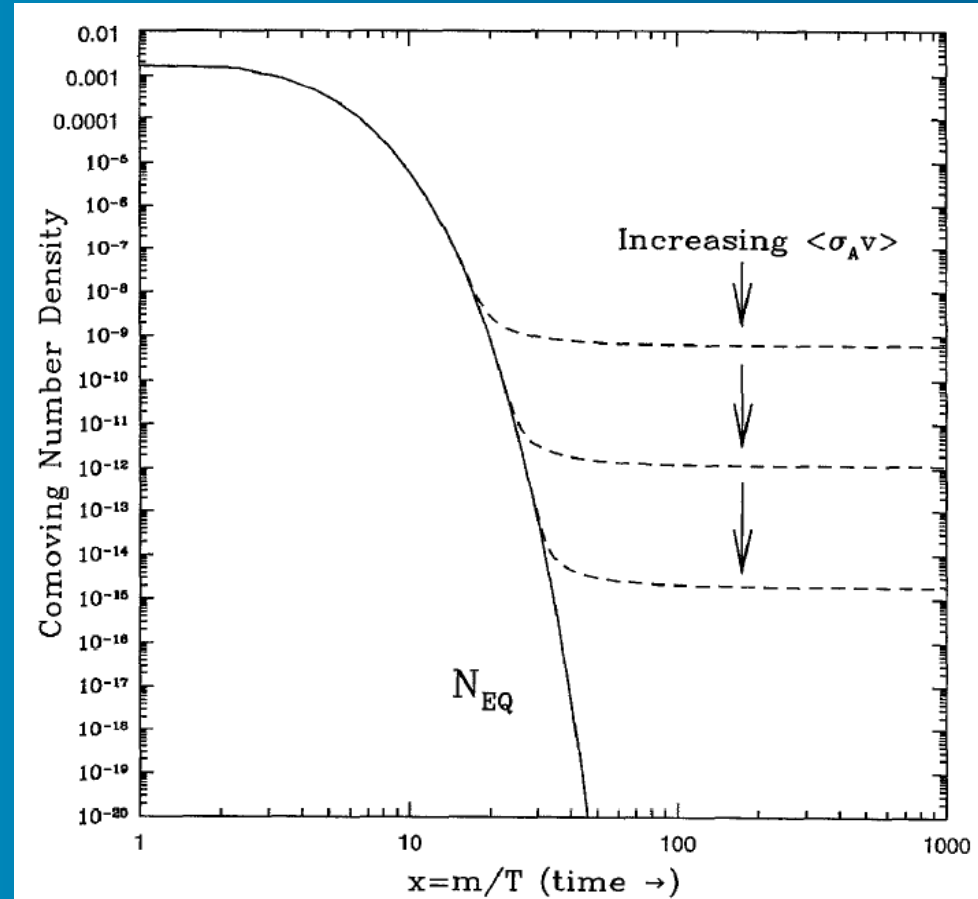
$$n_\chi \sim \frac{3H}{\langle\sigma v\rangle} \Big|_{\text{freezeout}}$$

$$T_{\text{Freezeout}} \sim m_\chi / 30$$

$$\Omega_\chi h^2 \sim 0.1 \left(\frac{\langle\sigma v\rangle}{\left(0.1/\text{TeV}\right)^2} \right)$$

Ω does not depend on m

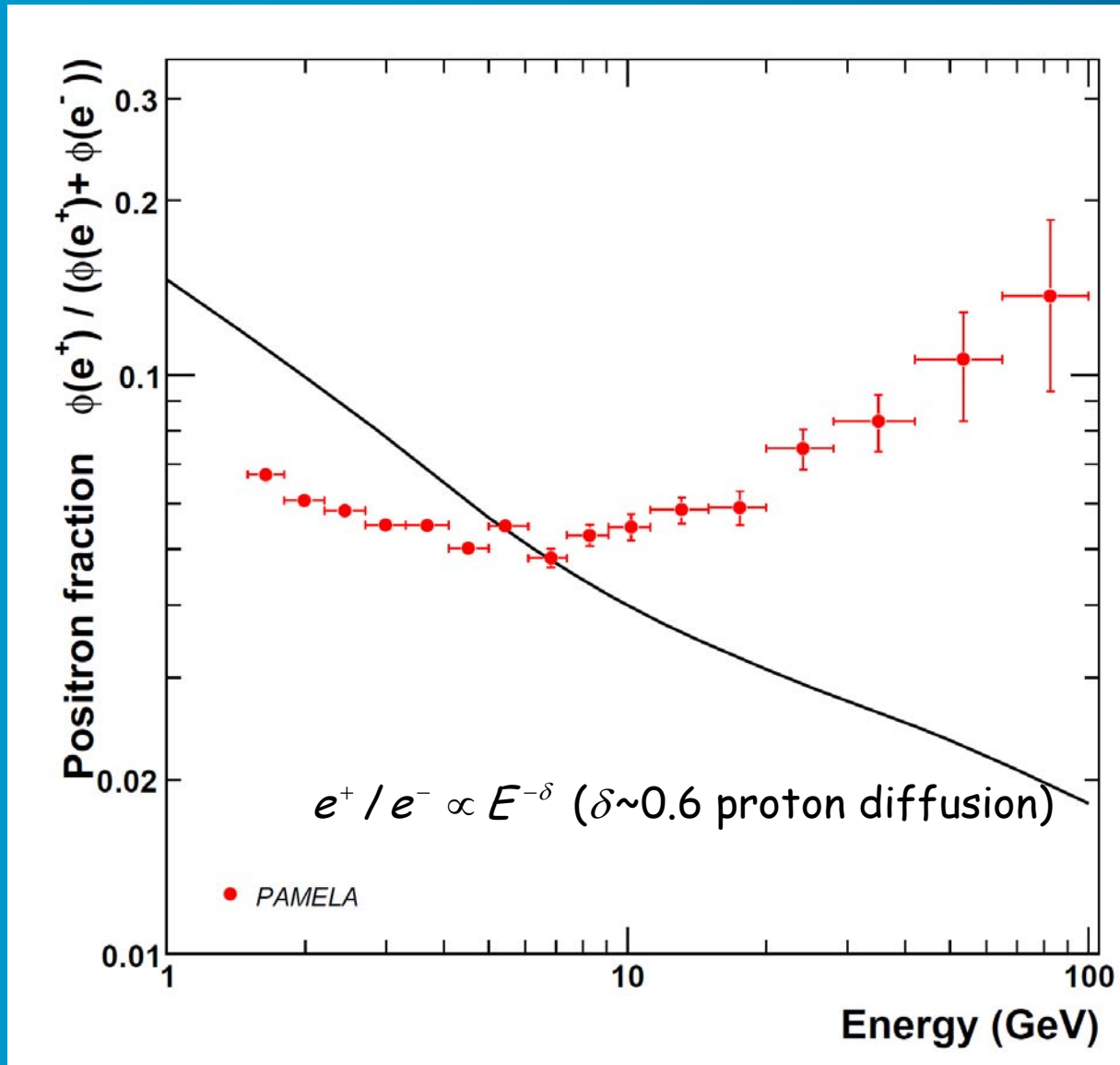
Predicting TeV Physics!!!



Kolb & Turner

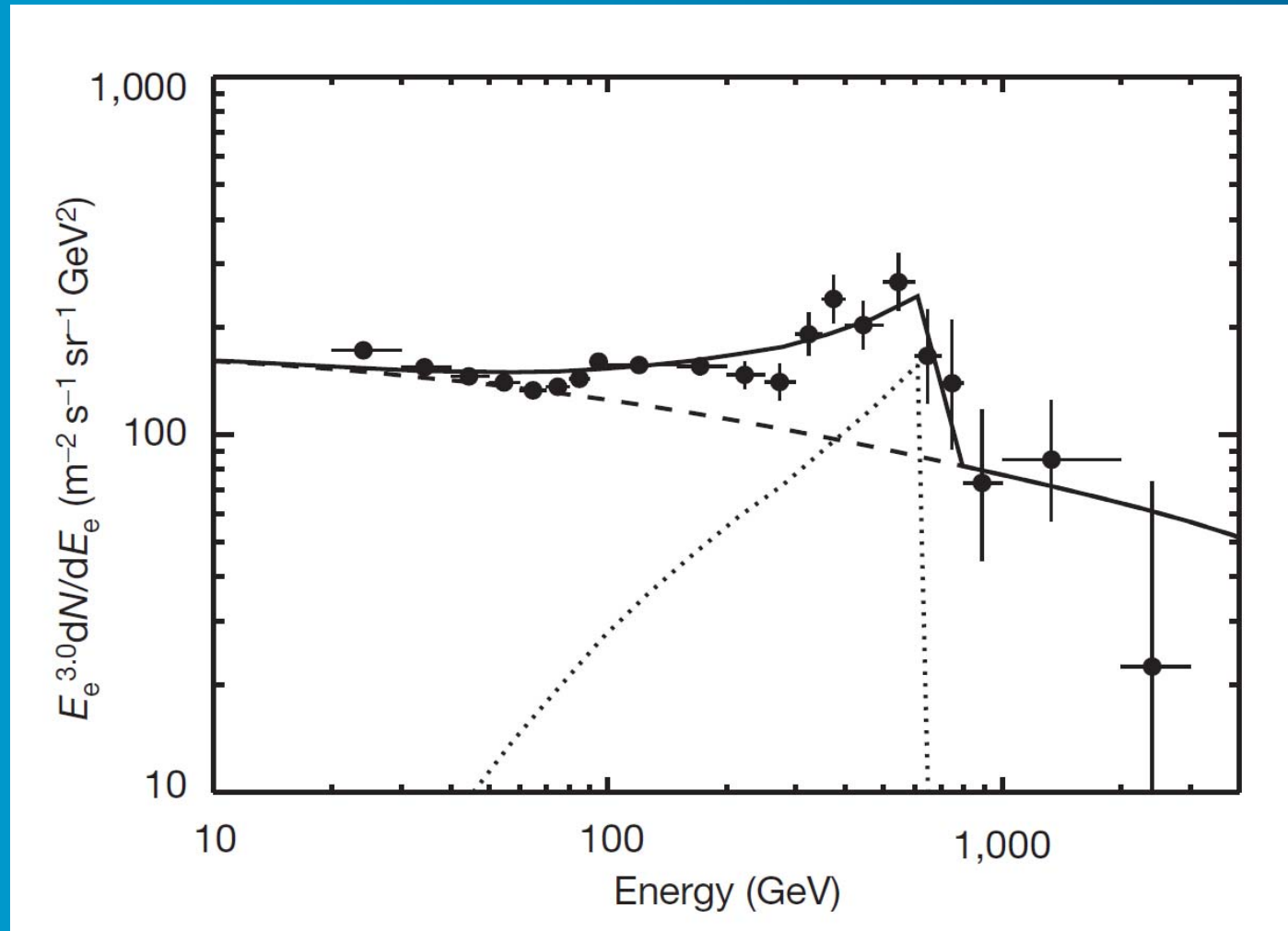
$$\langle\sigma v\rangle = 3 \times 10^{-26} \text{ cm}^3 / \text{s}$$

Positron Excess (PAMELA satellite reported)



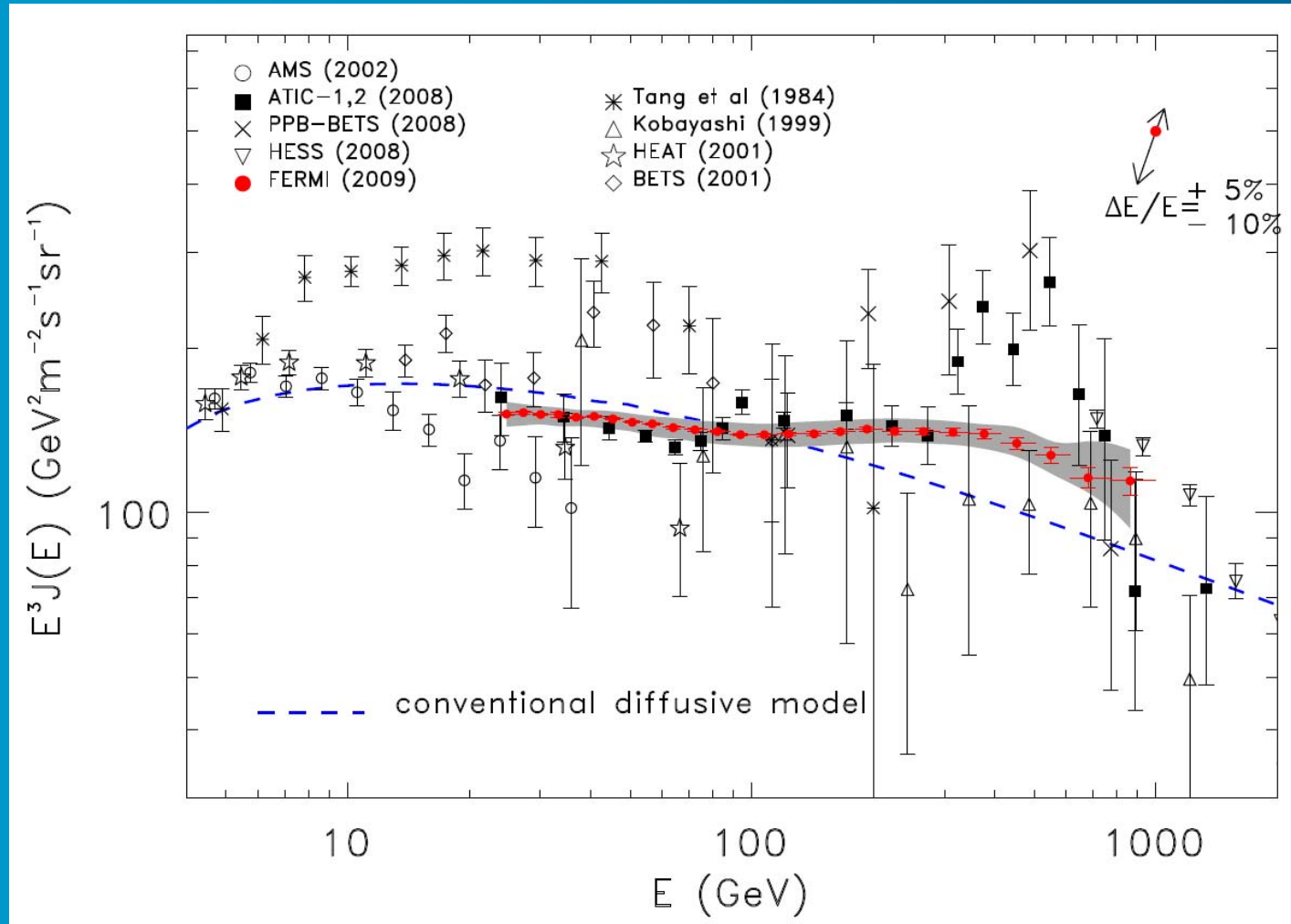
Adriani et al, [arXiv:0810.4995v1](https://arxiv.org/abs/0810.4995v1) [astro-ph]

Electron and positron flux by ATIC2



Chang et al (08)

Electron and positron flux by Fermi

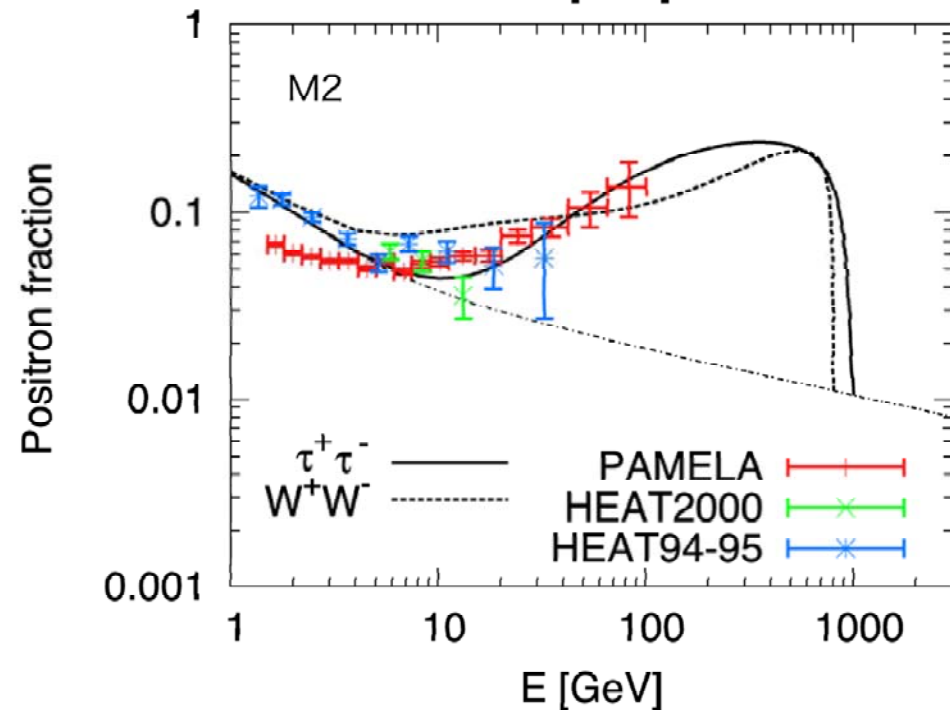
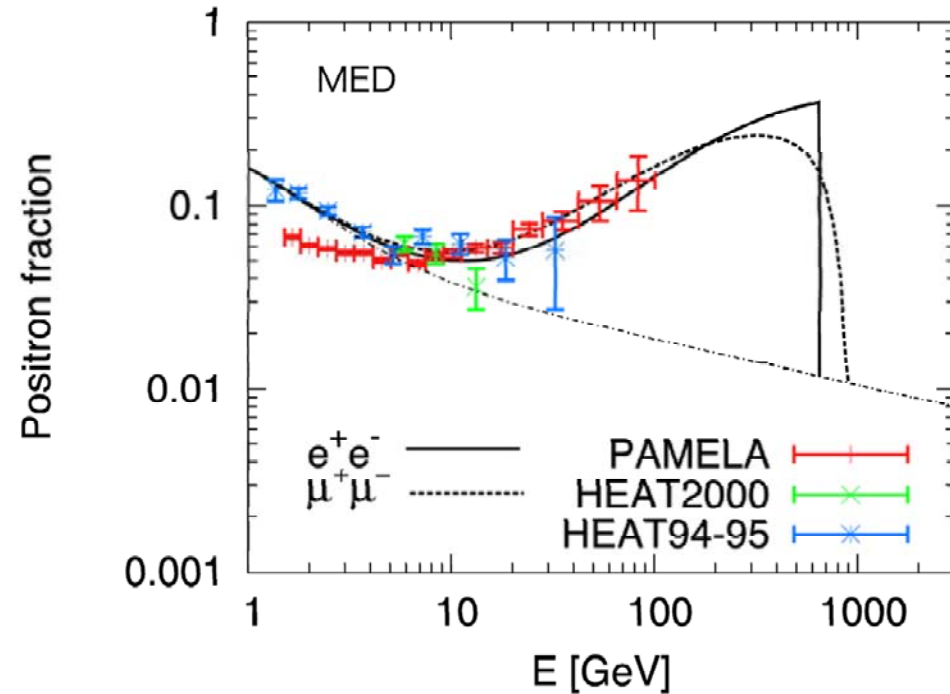


Positron excess in DM annihilation

Hisano, Kawasaki,
Kohri, Moroi, Nakayama (09)

Diffusion model
Fitted to B/C ratio

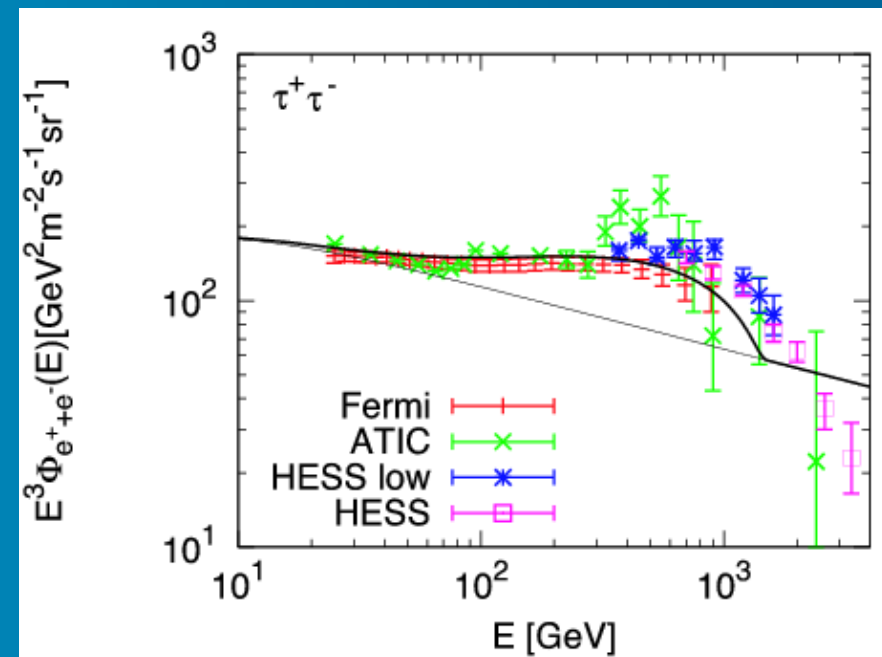
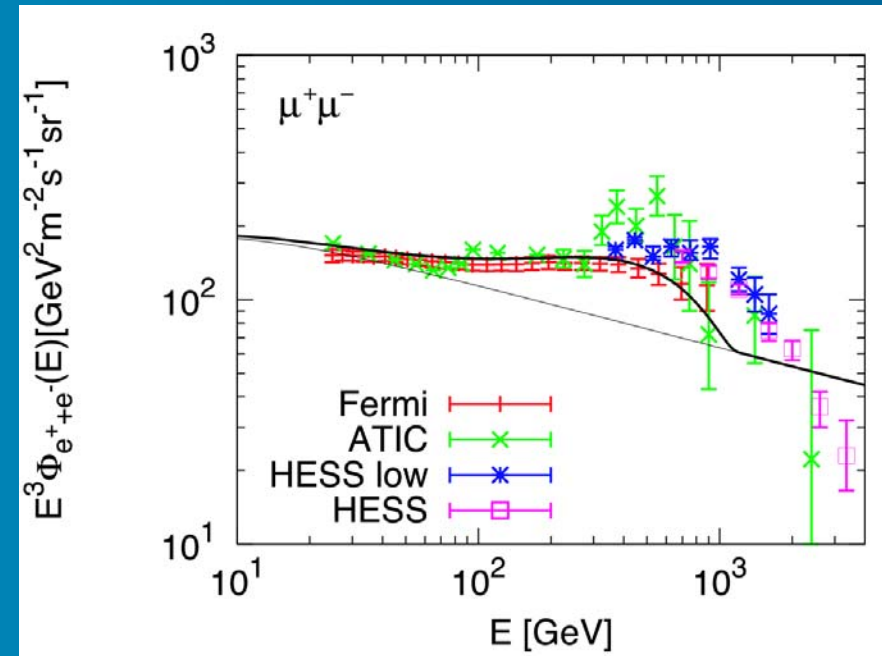
$$\langle \sigma v \rangle \sim 10^{-24} - 10^{-23} \text{ cm}^3 / \text{s}$$



Electron/positron cutoff in DM annihilation

Hisano, Kawasaki,
Kohri, Moroi, Nakayama (09)

$$\langle \sigma v \rangle \sim 10^{-23} \text{ cm}^3 / \text{s}$$

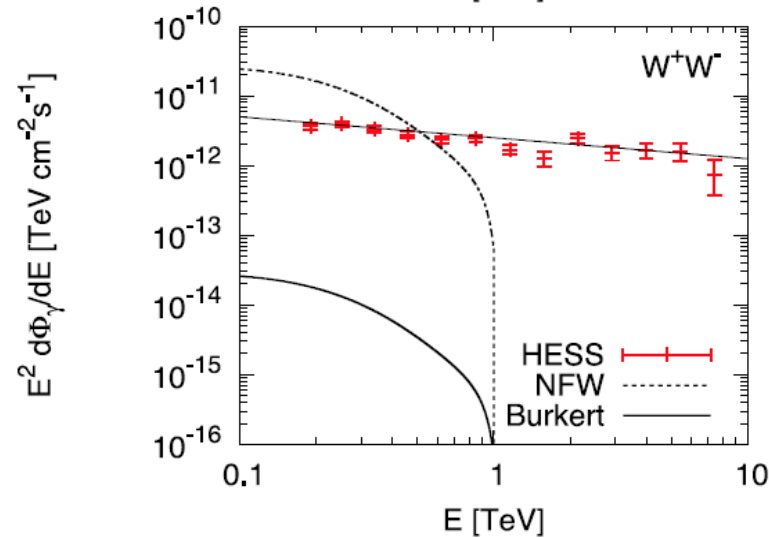
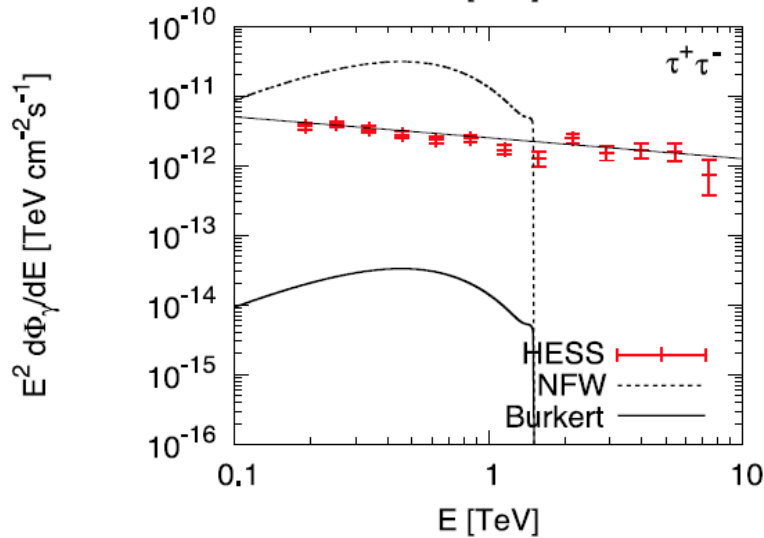
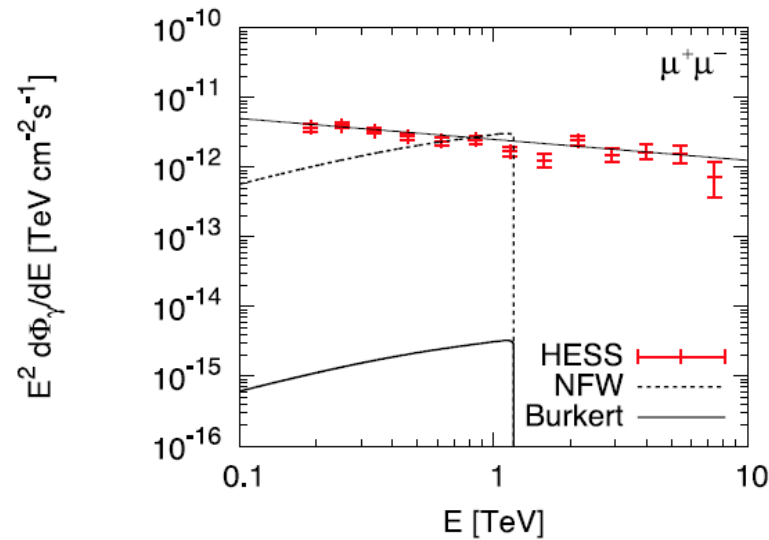
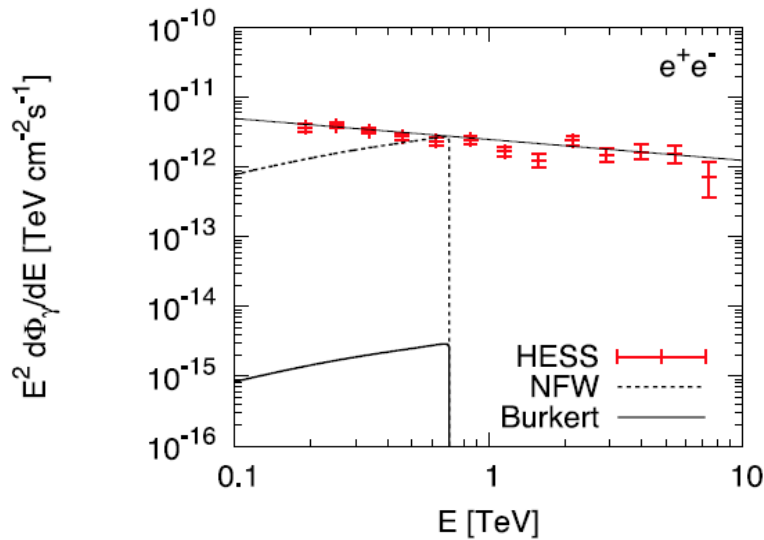


Gamma-ray signal from GC by DM annihilation

Kawasaki, Kohri, Nakayama (09)

Burkert profile [28]

$$d_{\text{Bur}}(x) = \frac{1}{(1+x)(1+x^2)}.$$



Extragalactic diffuse Gamma-ray by DM annihilation

Kawasaki, Kohri, Nakayama (09)

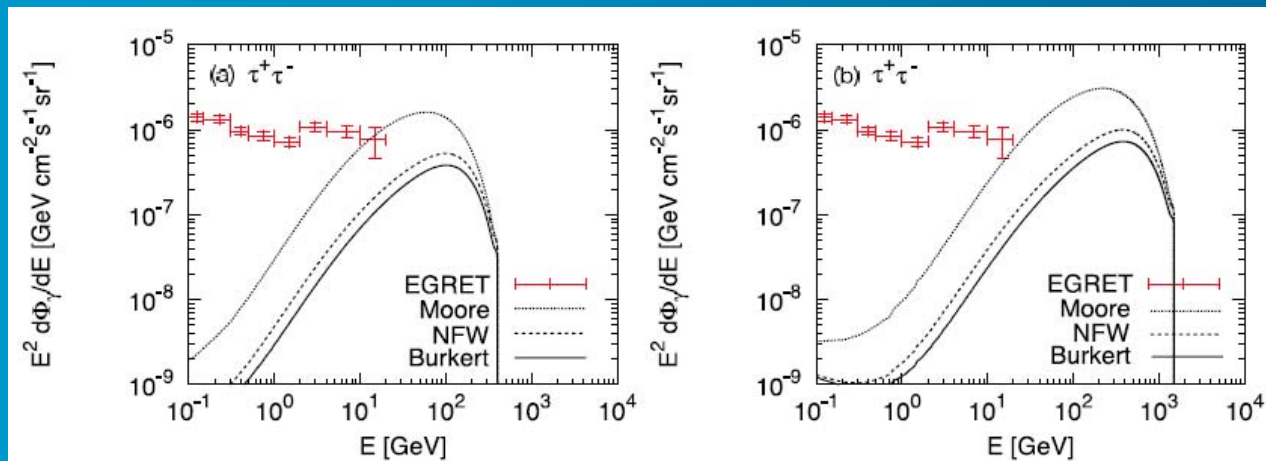


Figure 9: Same as Fig. 7, but for DM annihilating into $\tau^+\tau^-$.

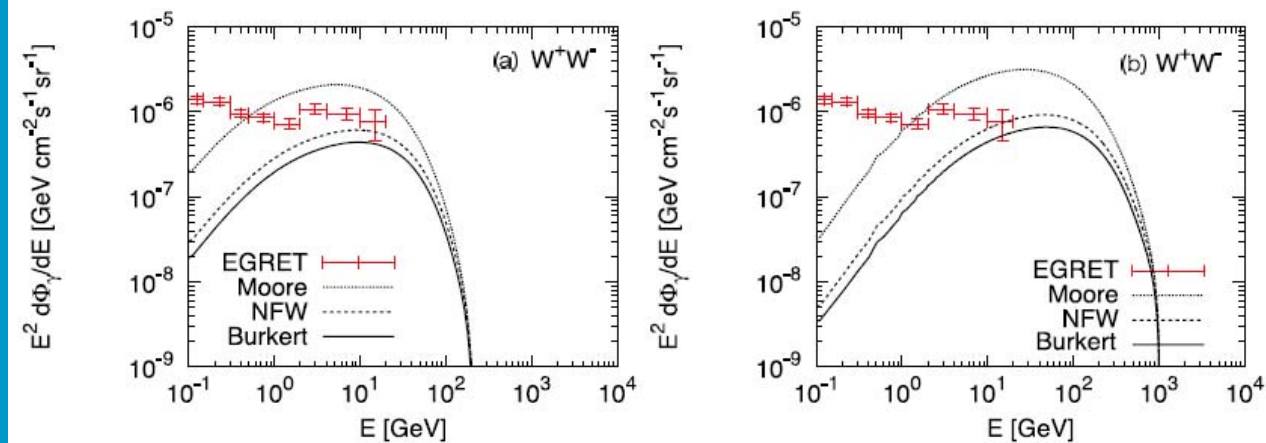


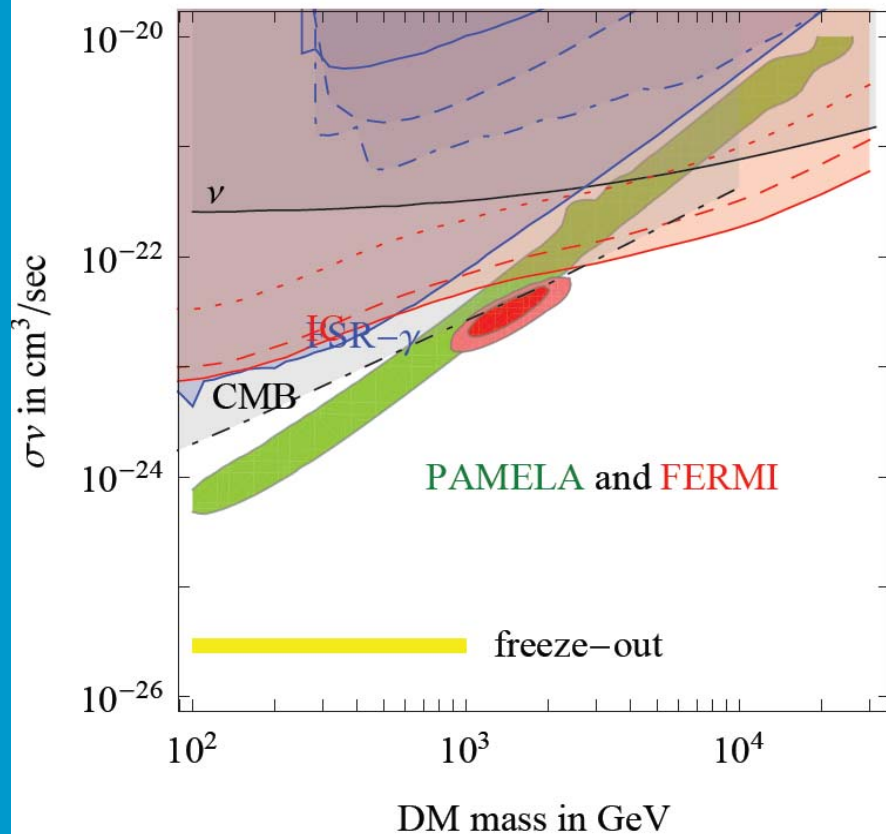
Figure 10: Same as Fig. 7, but for DM annihilating into W^+W^- .

Fitting by Papucci and Strumia

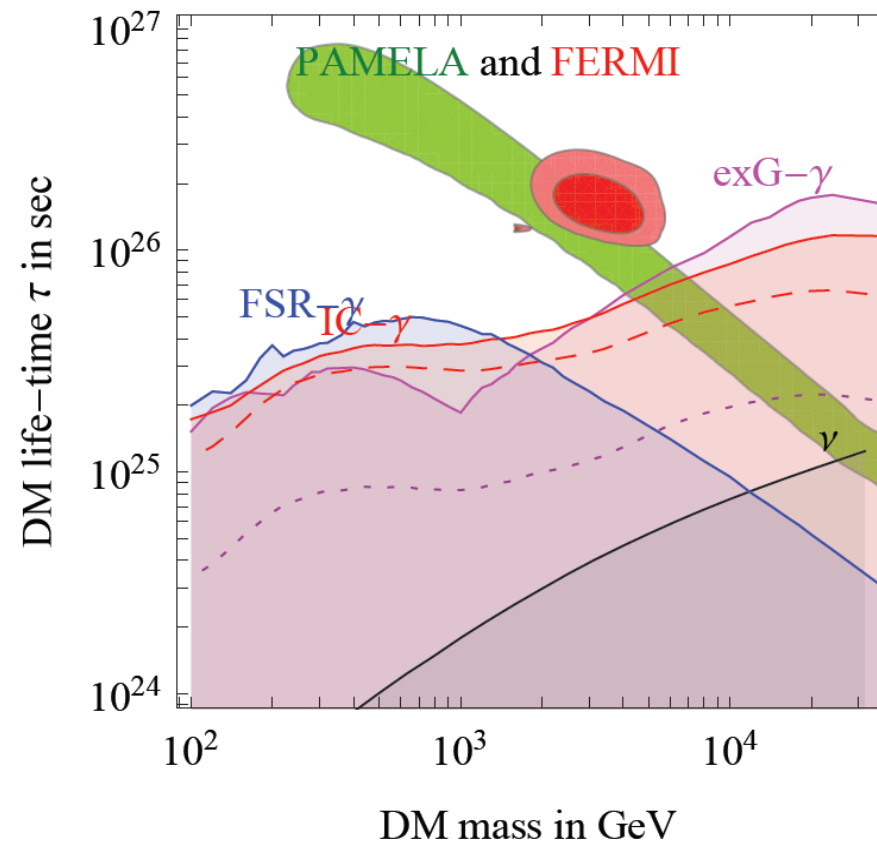
Papucci, Strumia, arXiv:0912.0742 [hep-ph]

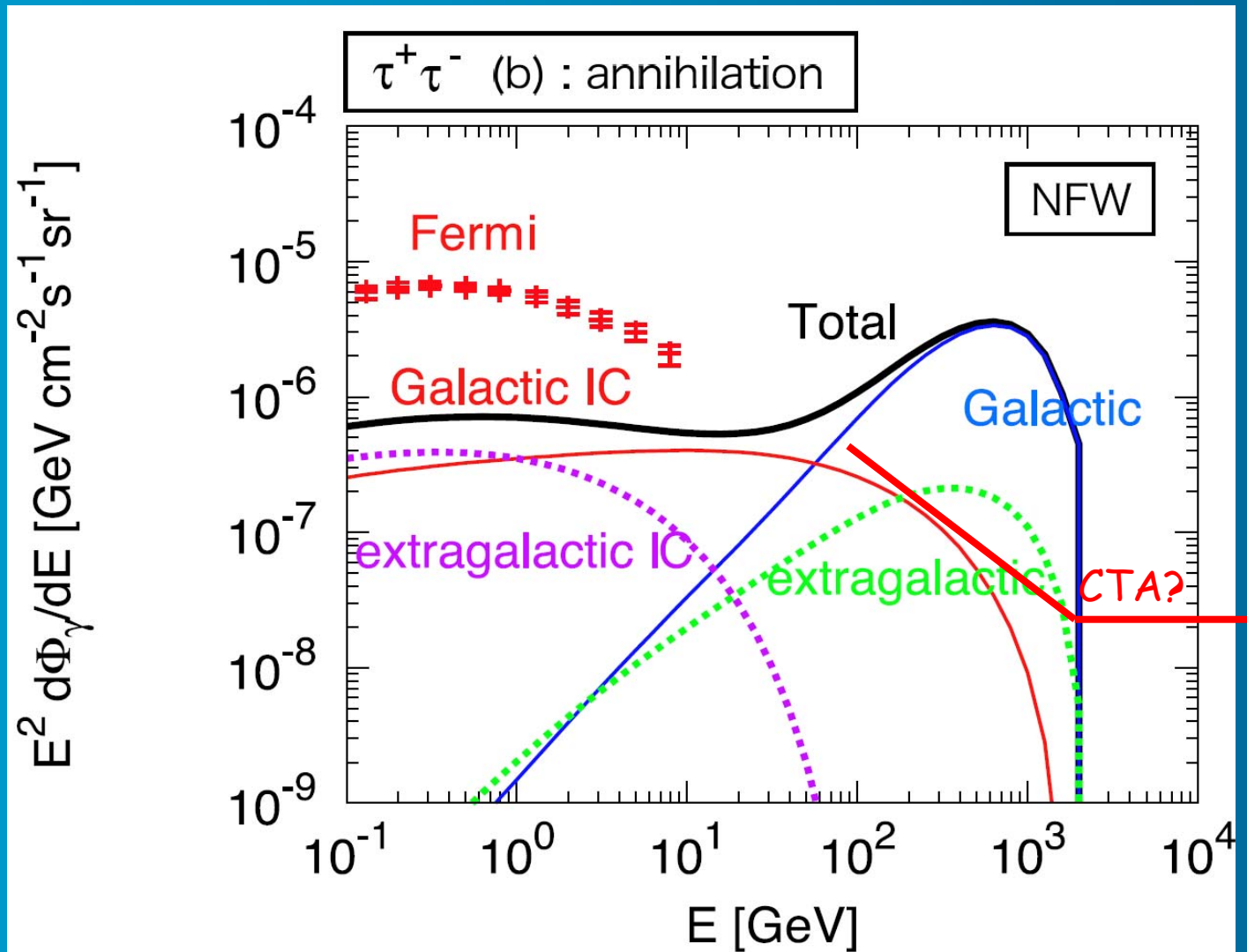
See also Chen, Mandal and F. Takahashi, arXiv:0910.2639 [hep-ph]

DM DM $\rightarrow \mu^+ \mu^-$, isothermal profile



DM $\rightarrow \mu^+ \mu^-$, NFW profile

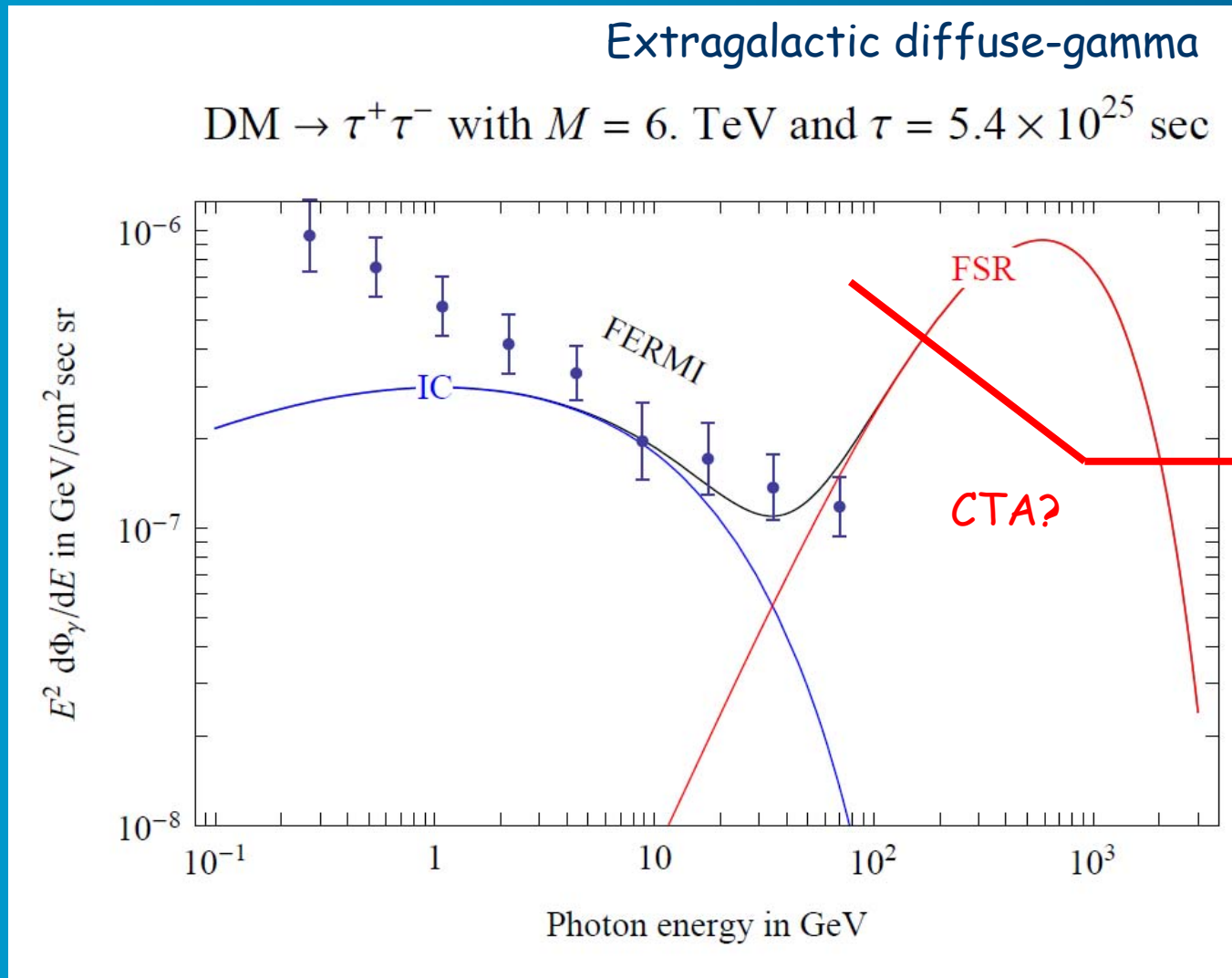




Courtesy of Kazunori Nakayama

Result of Papucci and Strumia

Papucci, Strumia, arXiv:0912.0742v1 [hep-ph]



Direct detection by CDMSII

arXiv:0912.3592v1 [astro-ph.CO]

Background

0.8 0.1(stat) 0.2(syst)

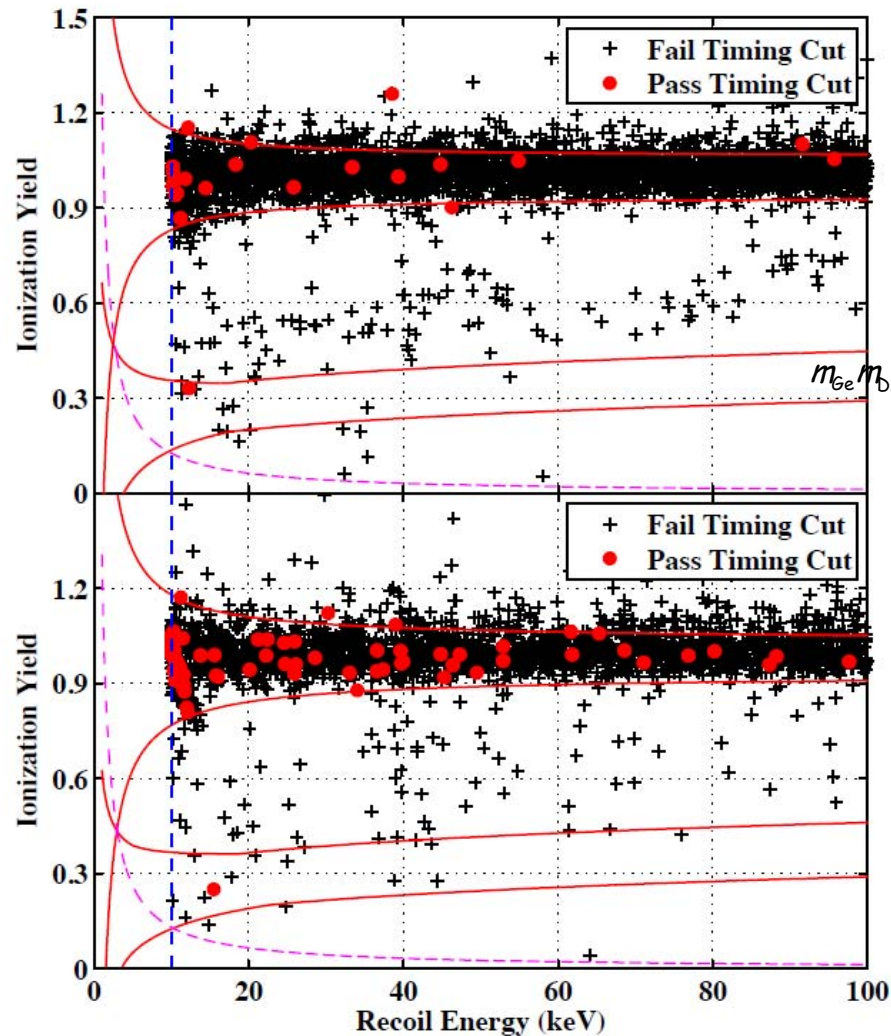
$$E_{\text{recoil}} \sim \frac{1}{2} \mu v^2 \sim O(10) \text{keV}$$

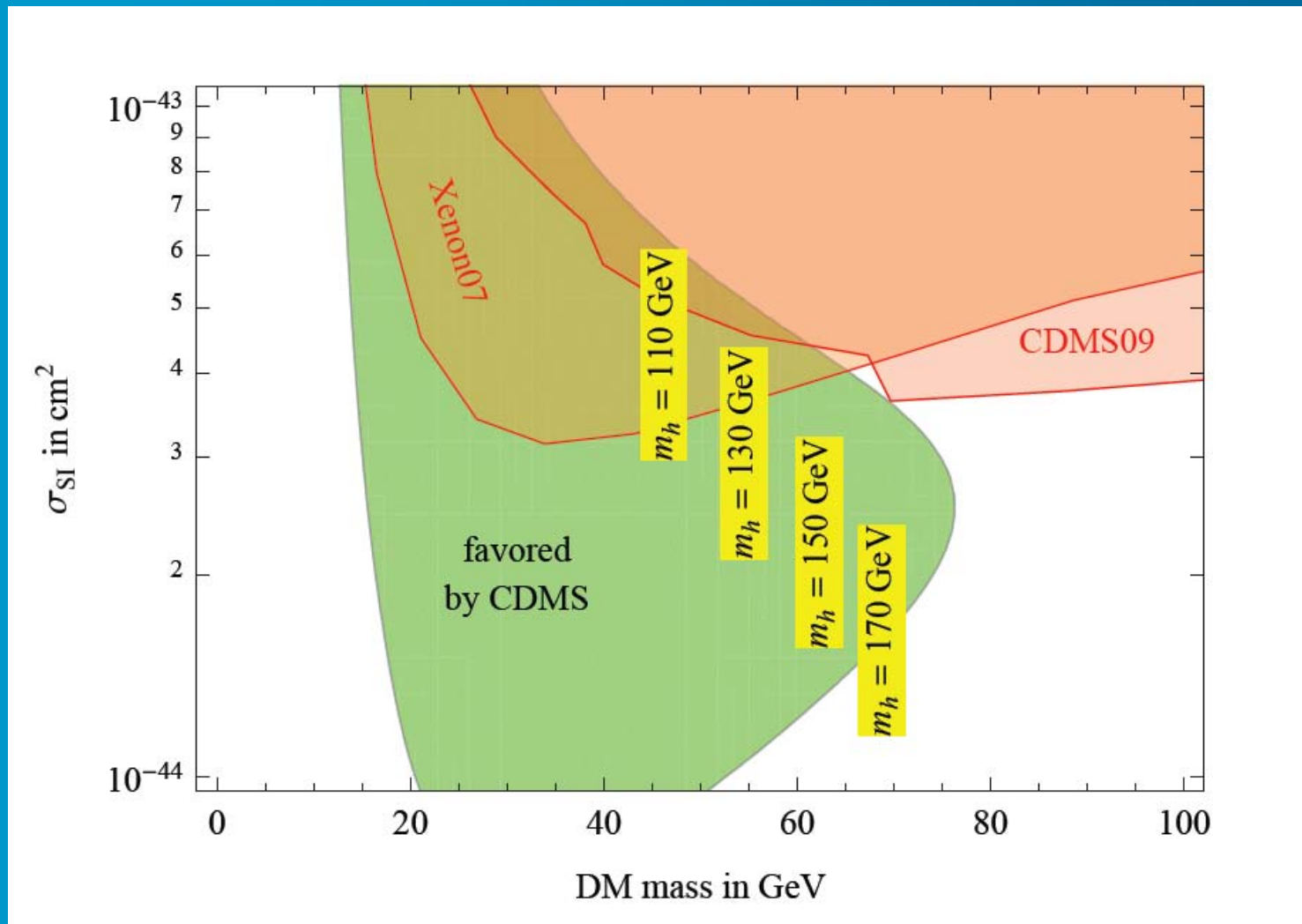
$$v \sim 220 \text{km/s} (v/c \sim 10^{-3})$$

$$\mu \sim \frac{m_{\text{Ge}} m_{\text{DM}}}{m_{\text{Ge}} + m_{\text{DM}}}$$

$$m_{\text{Ge}} = 72.6 \text{ u}$$

$M < O(100) \text{ GeV?}$ (Farina et al)





Conclusion

- Fermi may not exclude the possible scenarios for the positron/electron excess by the DM annihilation/decay because of the upper limit on the sensitivity ($<300 \text{ GeV}$)
- CTA will be able to verify those scenarios
- CTA may have a sufficient sensitivity to detect gamma-rays associated with DM annihilation even with its canonical annihilation cross section ($\sim 3 \cdot 10^{-26} \text{ cm}^3/\text{s}$)